

Pictures **NOT** accurately drawn

A 20 Euro note is a rectangle 133 mm long and 72 mm wide. A 500 Euro Note is a rectangle 160 mm long and 82 mm wide.

Show that the two rectangles are **not** mathematically similar.

(Total 3 marks)



The diagram shows a circle, centre O.

AC is a diameter. Angle $BAC = 35^{\circ}$. D is the point on AC such that angle BDA is a right angle.

.....° (2)

(b) Calculate the size of angle *DBC*.

.....° (1)

⁽a) Work out the size of angle *BCA*. Give reasons for your answer.

(2)

Calculate the size of angle *BOA*. (c)

> • (Total 5 marks)

3. PQRS is a quadrilateral.



PQ is parallel to SR. SP is parallel to RQ.

Prove that triangle PQS is congruent to triangle RSQ. (a)

(3)

In quadrilateral PQRS, angle SPQ is obtuse. (b) Explain why PQRS cannot be a cyclic quadrilateral.

> (2) (Total 5 marks)



Diagram NOT accurately drawn

Two cylinders, **P** and **Q**, are mathematically similar.

The total surface area of cylinder **P** is 90π cm².

The total surface area of cylinder **Q** is 810π cm².

The length of cylinder **P** is 4 cm.

(a) Work out the length of cylinder **Q**.

..... cm

The volume of cylinder **P** is 100π cm³.

(b) Work out the volume of cylinder **Q**. Give your answer as a multiple of π .

..... cm³ (2) (Total 5 marks)



Diagram NOT accurately drawn

The radius of the base of a cone is x cm and its height is h cm.

The radius of a sphere is 2x cm.

The volume of the cone and the volume of the sphere are equal.

Express h in terms of x.

Give your answer in its simplest form.



ABC is an equilateral triangle. *AD* is the perpendicular bisector of *BC*. *BX* is the angle bisector of angle *ABC*.

(a) Show that triangle *BXD* is similar to triangle *ACD*.

(2)

Edexcel GCSE Maths - Geometrical Reasoning (H)

In triangle ACD, AC = 2 cm, $AD = \sqrt{3} \text{ cm}.$

(b) Show that
$$XD = \frac{1}{\sqrt{3}}$$
 cm



7.



AB is parallel to DE. ACE and BCD are straight lines. AB = 6 cm, AC = 8 cm, CD = 13.5 cm, DE = 9 cm. (i) Work out the length of *CE*.

..... cm

(ii) Work out the length of *BC*.

.....cm (Total 3 marks)



The two triangles ABC and PQR are mathematically similar.

Angle A = angle P. Angle B = angle Q. AB = 8 cm. AC = 26 cm. PQ = 12 cm. QR = 45 cm.

(a) Work out the length of *PR*.

.....cm

(b) Work out the length of *BC*.

.....cm

(2) (Total 4 marks)

(2)





(a) Prove that triangle *ECD* is congruent to triangle *BCF*.

G is the point such that *BEGF* is a parallelogram.

(b) Prove that ED = EG

(2) (Total 5 marks)

(3)



Diagram **NOT** accurately drawn

Triangle PQR is isosceles with PQ = PR. X is a point on PQ. Y is a point on PR. PX = PY.

Prove that triangle *PQY* is congruent to triangle *PRX*.

(Total 3 marks)



Diagram NOT accurately drawn

In the diagram Q and R are points on the circumference of a circle. TQ and TR are tangents to the circle. PQ = PR. Angle RQT = angle QRT = 70°. Angle RPQ = 120°.

Explain why *P* is not the centre of the circle.



P and Q are two points on a circle centre O.

The tangents to the circle at P and Q intersect at the point T.

(a) Write down the size of angle *OQT*.

(b) Calculate the size of the obtuse angle *POQ*.

°

•

(2)

(1)

3

(2)

- Give reasons why angle PQT is 70° (c) (Total 5 marks)
- 1.84.. ≠ 1.95.. 1.20.. ≠ 1.13.. $\frac{133}{72} = 1.8472$, $\frac{160}{82} = 1.9512$ OR $\frac{72}{133} = 0.54135, \frac{82}{160} = 0.5125$ OR $\frac{160}{133} = 1.203...., \frac{82}{72} = 1.1388....$ OR $\frac{133}{160} = 0.83125..., \frac{72}{82} = 0.878$ *M1 for* $\frac{133}{72}$ (= 1.8472...) *oe Accept 1.8, 1.85 M1 for* $\frac{160}{82}$ (= 1.9512...) *oe consistent pairing* Accept 2.0, 1.9 **OR** M1 for $\frac{160}{133}$ (= 1.203...) oe *M1 for* $\frac{82}{72}$ (= 1.1388) *oe* Al for enough decimal places to show that the ratios are not equal; since the scale factors are different the shapes cannot be similar. NB Do Not need conclusion

[3]

2.	(a)	55°	2		
		$90-35 = 55^{\circ}$			
		Angle in a semi-circle = 90°			
		B1 for 55° B1 for (angle in) a semi-circle = 90°			
	(b)	3.50	1		
	(0)	55 00 "55"	1		
		$90 - 55^{\circ}$ B1 for 35° ft			
	(c)	110°	2		
		$180 - 2 \times 35 = 110^{\circ}$			
		M1 for complete method or for twice "(a)" $A1$ cao			
		Candidates may choose to use Isosceles triangles or			
		Angle subtended at centre is twice angle subtended at			
		circumference			
				[5]	
3.	(a)	Angle $PQS = QSR$			
		Angle $RQS = PSQ$			
		SQ is common	2		
		$\frac{Bl \text{ for } l \text{ condition} + reason}{Bl \text{ for } l \text{ condition} + reason}$	3		
		B1 for 2^{nd} condition + reason			
		B1 for 3^{rd} condition + reason + statement of congruency			
	(1-)				
	(0)	2 obtuse angle added are $> 180^{\circ}$ therefore they cannot			
		add up to 180 therefore the shape cannot be cyclic	2		
		B1 for states P and R are both obtuse			
		B1 sum greater than 180 for angles P and R or less than 180 for angles Q and S			
		jor angles Q ana S		[6]	
				[5]	

4. (a) 12 $\frac{810\pi}{90\pi} \text{ or } 9$ $\sqrt{9} \text{ or } 3$ $M1 \text{ for } \frac{810\pi}{90\pi} \text{ or } 9 \text{ or } \frac{1}{9} \text{ or } 1:9 \text{ oe}$ $M1 \text{ for } \sqrt{\frac{810\pi}{90\pi}} \text{ or } \sqrt{9} \text{ or } 3 \text{ or } \frac{1}{3} \text{ or } \sqrt{9} : \sqrt{1} \text{ oe}$ A1 cao SC:B1 for answer of 36

(b)
$$2700\pi$$
 2
 3^3 or 27 or 2700

M1 for "3"³ or 27 or
$$(\sqrt{9})^3$$
 : $(\sqrt{81})^3$ *oe or 9³ or 2700–*
A1 cao

3

2

[5]

[3]

32x

$$\frac{1}{3}\pi x^{2}h = \frac{4}{3}\pi (2x)^{3}$$

$$x^{2}h = 4 \times 8x^{3}$$
M1 for substitution in correct formulae
M1 (dep.) for correct unsimplified expression eg

$$h = \frac{\frac{4}{3}\pi (2x)^{3}}{\frac{1}{3}\pi x^{2}} oe or h = 8x oe$$
1 for 32x cao

6. (a) Angle BDX = angle ADC = 90° Angle BXD = angle ACD = 60° Hence similar B2 for 2 of (Angle BDX = angle ADC, Angle BXD = angle ACD, angle DAC = angle DBX) B1 for 1 of the above

5.

(b)
$$\frac{XD}{DC} = \frac{BD}{AD}$$
, $DC = BD = 1$
 $MI \frac{XD}{DC} = \frac{BD}{AD}$ or $\frac{XD}{BD} = \frac{DC}{AD}$ or a statement that ACD is an
enlargement of BDX, scale factor $\sqrt{3}$
 $AI \frac{XD}{I} = \frac{1}{\sqrt{3}}$
 $AI XD = \frac{1}{\sqrt{3}}$

7.
$$\frac{CE}{8} = \frac{9}{6} \text{ or } \frac{CE}{9} = \frac{8}{6} \Rightarrow CE = \frac{8 \times 9}{6}$$
$$\frac{BC}{13.5} = \frac{6}{9} \text{ or } \frac{BC}{6} = \frac{13.5}{9} \Rightarrow BC = \frac{13.5 \times 6}{9}$$
(i) 12
(i) 12
(ii) 9
$$MI \text{ for scale factor } \frac{9}{6} \left(\text{ or } \frac{6}{9} \right) \text{ or } \frac{8}{6} \left(\text{ or } \frac{6}{8} \right) \text{ or } \frac{13.5}{9} \left(\text{ or } \frac{9}{13.5} \right) \text{ oe}$$
$$AI \text{ cao for } 12$$
$$AI \text{ cao for } 9$$

[3]

2

2

[5]

8. (a) SF = 1.539 cm

$$MI SF = \frac{12}{8}, \frac{8}{12}, 1.5, 0.6 \dots oe$$

Al cao

- (b) $45 \times \frac{8}{12}$ 30cm
- $M1 \ 45 \times \frac{8}{12}, \ 45 \div \frac{12}{8} \ oe$ A1 cao

[4]

9.	(a) $BC = CE$ e CF = CD e BCF = DC BFC is con	equal sides equal sides $E = 150^{\circ}$ figruent to ECD (SAS) B1 for either BC = CD or BC = CE CF = CE or $CF = CDB1 for BCF = DCE = 150° or correct reasonB1 for proof of congruence$	3	
	(b) So $BF = ED$ BF = EG (c)	D (congruent triangles) opp sides of parallelogram) BI BF = EG or BF = ED BI fully correct proof	2	[5]
10.	PQ = PR given PY = PX given Angle P common SAS	M1 for $PQ = PR$ with reason or $PY = PX$ with reason M1 for P identified as a common angle A1 for completion of proof and SAS	3	[3]
11.	$\frac{1}{2}(180 - 120) = 3$ Angle <i>PQR</i> = 30°	0° P so PQ is not a radius M1 for angle between tangent and radius is 90° or sight of right angle marked on diagram A1 for angle PQR = 30° not 20° or angle PQT = 100° not 90° or QTR = 40° not 60°	2	[2]
12.	(a) 90(b) 140	B1 cao M1 for sight of 20° or 360 – 90 – 90 – 40 A1 for 140°	1 2	

2

(c)

B1 for Angle between <u>tangent</u> and <u>radius</u> = <u>90°</u> or <u>Tangents</u> from a <u>point</u> to a circle are <u>equal</u> B1 for <u>Isosceles</u> triangle POQ so angle OQP = 20°or Angles in a triangle add up to 180°

[5]

1. Mathematics A

Paper 4

Most answers showed no understanding of mathematical similarity, most making some comparison of areas or perimeters, or subtracted the lengths of the sides. Of those who did attempt a division, most gained the full marks, since they were then able to justify their results in the context of the question.

Paper 6

Candidates did well on this unusual question. There were many successful approaches involving the calculation of appropriate scale factors and showing that they were not equal. Almost as popular was to calculate a scale factor from say 160/133 and then multiplying 72 by this and showing the answer was not equal to 82.

Mathematics B Paper 17

The great majority of candidates did not understand the concept of similarity. Many simply worked out the areas of the two notes, offering no explanation. Some tried to use the monetary value of the notes to disprove similarity. A few did calculate ratios and explain their findings well.

2. Paper 3

In part (a) many candidates worked out the size of angle *BCA as* 55° but very few gave a valid reason. Part (b) was often done well, even after an incorrect part (a). Part (c) was answered less well with many candidates failing to realise that they were dealing with an isosceles triangle. A significant number of candidates did not appear to be familiar with angle notation and did not appreciate which angle they were expected to find in each part of this question.

Paper 5

There was an improvement in the performance of candidates in this circle geometry question. 80% of candidates were able to calculate the missing angle in part (a) and about half of these candidates were able to correctly state a reason for their answer. Part (b) was also well answered with again 80% of candidates able to work out the correct answer. Part (c) was not so well answered as candidates had to make two steps in their solution. Only 57% of candidates were successful in this part.

3. Only 7% of candidates were able to give a full solution to proving that the two triangles were congruent in part (a); they often took for granted what they were trying to prove. In part (b) candidates did not give sufficient reasons as to why two obtuse angles had a swn of greater than 180° though 20% of candidates gave a complete solution and a further 10% a partial solution,

4. Specification A

Most candidates attempted this question but only the best were able to achieve full marks. By far the most common answer to part (a) was 36, and to part (b) was 900 π . In part (b), some candidates were able to score a mark for cubing the scale factor they derived in part (a). A small number of candidates calculated the radius of *P* to deduce the radius, and hence the volume, of *Q*. A significant proportion of those candidates getting as far as the volume 2700 π did not understand the demand of the question and omitted to include the π in their final answer.

Specification B

The most commonly seen answer to this question was 36 in (a) and 900π in (b). These were both incorrect solutions and occurred when candidates mistakenly used the area scale factor as the length and then volume scale factor. A small minority of candidates were able to often fully correct solutions although the omission of π from the answer to (b) resulted in some candidates failing to gain the final accuracy mark. There was evidence of some poor arithmetic in this question with 810 divided by 90 being evaluated as 90.

5. Specification A

Although there were few completely correct answers to this question, many candidates scored at least one mark for correctly using the equations for the cone and sphere. A typical candidate substituted x into the equation for the cone, 2x into the equation for the sphere, forgot to cube the 2 and, after rearrangement, arrived at an answer 8x.

There were a surprising number of candidates who, having started correctly with $\frac{1}{3}\pi x^2 h =$

$$\frac{4}{3}\pi(2x)^3$$
, than incorrectly subtract the fractions to get $\pi x^2 h = 1\pi(2x)^3$.

Specification B

Approximately two thirds of candidates were able to substitute the given radii into the correct formulae. The formula for the surface area of a sphere was sometimes used instead of the

formula for the volume. The most common error on substituting the radii was to give $\frac{4}{3}p2x^3$

instead of the correct $\frac{4}{3}p(2x)^3$. Candidate who made this error lost one mark out of the available three provided they managed to make *h* the subject of their formula using correct algebraic processes. The level of algebra was generally very poor with very few candidates being able to carry out what should have been a straightforward division. The most common error here was to subtract $\frac{1}{3}$ from either side of the equation rather than multiply by 3.

6. There was a great deal of confusion between conditions for similarity and conditions for congruence., with such 'explanations' as 'Angle, angle, side' or 'right angle, hypotenuse and angle' being quoted. It was a pleasure to see good attempts at part (b), mainly using the similarity established in part (a) but with a few using the fact that $\tan 30^\circ = \frac{1}{\sqrt{3}}$ which can be obtained from triangle *ADC*.

obtained from thangle ADC

7. Intermediate Tier

This question was answered poorly. Candidates either have very little understanding of similar triangles or fail to recognize them when they appear. Many gave the two lengths as 13.5 cm and 8 cm (assuming the triangles to be isosceles) and some attempted to use Pythagoras' theorem. About 10% of candidates got at least one length correct but few wrote down a scale factor.

Higher Tier

Many candidates did well on this question. Most were able to match the triangles to derive the appropriate ratios. Generally candidates who could do (i) could also do (ii). There were a relatively small number of candidates who attempted to use Pythagoras' theorem or the cosine rule for the lengths.

8. Specification A

Intermediate Tier

The common approach to this question was to assume that values were added on to give the enlarged triangle, rather than the adoption of an approach which involved factors. A few attempted to apply Pythagoras. Credit was available for finding factors alone, but there was little evidence to substantiate the award of these method marks. It was clear that most candidates failed to associate "similar" with scale factors.

Higher Tier

Many candidates scored full marks on this question, and there were relatively few incorrect methods involving Pythagoras' theorem. Common mistakes occurred in simplifying the scale factor $\frac{12}{8}$ to $\frac{4}{3}$ or 1.4; and in part (b), errors in calculating $45 \div 1.5$. Some of the weaker candidates, not understanding the need for a scale factor, simply added 4 (derived from the difference of *PQ* and *AB*) to *AC* to obtain *RP* = 30.

Specification B

Intermediate tier

It was disappointing to see so many candidates merely adding or subtracting 4 cm from the given lengths to give answers of PR = 30 (26 + 4) and BC = 41 (45 - 4). A small number used RQ in (a) instead of (b), and AC likewise; they then contrived to get the desired results by wrongly manipulating the measurements given on the diagram. This gained no marks. Few candidates quoted any scale factor of enlargement although some did use the "once and a half again" method, usually to good effect. Very few quoted the equivalence of the ratios of corresponding sides. Quite a few tried to use Pythagoras ignoring that the question did not have right angled triangles.

- **9.** Setting out these proofs was not done well. Many used very wordy explanations rather than concise mathematical reasons and failed to identify the key stages required. About half the candidates were able to score at least one mark in part (a), usually for identifying a pair of equal sides in the triangles. Candidates often failed to give a reason for the equal angles (this was merely stated as fact), and some failed to identify the appropriate congruence. Generally part (b) was done a little better than part (a), but many candidates identified EDG as an equilateral triangle, or stated that EDF and EGF were identical isosceles triangles, without supporting evidence or explanation.
- 10. Few candidates understood the nature of proof. This question was very poorly done. it is important that candidates do recognise that they must qualify any statements they make. It was not sufficient to write PR = PQ without including that this was because triangle PQR was isosceles or that the information was given.
- 11. This question was very poorly answered with 80% of candidates scoring no marks. It was a pleasant surprise when candidates knew what they were talking about and managed to convey their ideas across...if not always eloquently. The tangent/ radius connection was often stated in about 10% of cases and most went on to discuss the 20°/30° situation, though some did get confused expecting the 70° to be 90°. Only 10% of candidates were able to produce a fully reasoned argument.

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12. It was disappointing to find that only just over half the candidates realised that angle OQT was 90°. This, in turn, went on to affect their calculations in part (b) as they could then have gone on to use the sum of the angles of the quadrilateral in an attempt to work out the size of angle POQ or recognise that OPQ was an isosceles triangle with the acute angles being 20° each. The mean mark for this part of the question was just under 1. Candidates often struggle to provide mathematical reasons for the size of an angle and this year was no exception with 0.37 being the mean mark for this part. Those who did score one of the marks tended to score it for mention of an isosceles triangle or for stating that the sum of the angles of a triangle is 180°. The few that did mention tangent theorems tended to talk about the angle between the tangent and the circle rather than the tangent and the radius.